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V. M. Tikhomirov tronslated by Abe Shenitzer

Throughout the history of mathematics, maximum and minimum problems have played an important role in the evolution of the field. Many beautiful and important problems have appeared in a variety of branches of mathematics and physics, as well as in other fields of sciences. The greatest scientists of the past-Euclid, Archimedes, Heron, the Bernoullis, Newton, and many otherstook part in seeking solutions to these concrete problems. The solutions stimulated the development of the theory, and, as a result, techniques were elaborated that made possible the solution of a tremendous variety of problems by a single method.

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# Mathematical Impressions 

## Anatolii T. Fomenko

"I think of my drawings as if they were photographs of a strange but real world, and the nature of this world, one of infinite objects and processes, is not well known. Clearly there is a connection between the mathematical world and the real world....This is the relationship I see between my drawings and mathematics."-Anatoliĭ Fomenko, in the Introduction

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